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 Testo A  
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\*\*\*\*\* Es 1.b

- Lineare se  $\eta=1$
- Stazionario se  $\rho=0$
- Istantaneo se  $\eta=0$

\*\*\*\*\* Es 1.c

$$P(s) = s^2 + 5s + 6 = (s+2)(s+3)$$

(i) modi aperiodici stabili

$$p1 = -2$$

modo  $\exp(-2t)$ ,  $\tau_{u1} = 0.5$ ,  $t_{a1} = 1.5$

$$p2 = -3$$

modo  $\exp(-3t)$ ,  $\tau_{u2} = 0.33$ ,  $t_{a2} = 1$

(ii)  
 Il modo piu' veloce è il secondo perché  
 $\tau_{u2} < \tau_{u1}$ .

\*\*\*\*\* Es 2

$$y_f(t) = 0.5t^2$$

\*\*\*\*\* Es 3

$$A = \begin{bmatrix} 0 & -6 \\ 1 & -5 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$C = \begin{bmatrix} 1 & 0 \end{bmatrix}$$

$$D = 0$$

Es 3.a

$$P(s) = P_{min}(s) = (s+2)(s+3)$$

Autovalori distinti ==> diagonalizzabile

\*\* Es 3.b

Matrice Modale

$$V = \begin{bmatrix} 3 & 2 \\ 1 & 1 \end{bmatrix}$$

$$V_{inv} = \begin{bmatrix} 1 & -2 \\ -1 & 3 \end{bmatrix}$$

$$A_{primo} = \begin{bmatrix} -2 & 0 \\ 0 & -3 \end{bmatrix}$$

$$B_{primo} = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$$

$$C_{primo} = \begin{bmatrix} 3 & 2 \end{bmatrix}$$

$$D_{primo} = 0$$

\*\* Es 3.c

$$e_{A'}t = \begin{bmatrix} \exp(-2t), & 0 \\ 0, & \exp(-3t) \end{bmatrix}$$

$$e_{At} = V * e_{A'}t * inv(V) =$$

$$\begin{bmatrix} 3e^{-2t} - 2e^{-3t}, & -6e^{-2t} + 6e^{-3t} \\ e^{-2t} - e^{-3t}, & -2e^{-2t} + 3e^{-3t} \end{bmatrix}$$

\*\* \*\* Es 3.d

$$x_{lib} = \begin{bmatrix} -9\exp(-2(t-1)) + 10\exp(-3(t-1)) \\ -3\exp(-2(t-1)) + 5\exp(-3(t-1)) \end{bmatrix}$$

$$y_{lib} = -9\exp(-2(t-1)) + 10\exp(-3(t-1))$$

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Testo B

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\*\*\*\*\* Es 1.b

- Lineare se  $\rho=1$
- Stazionario se  $\eta=0$
- Istantaneo se  $\rho=\eta=0$

\*\*\*\*\* Es 1.c

$$P(s)=s^2 + 5*s + 4 = (s+1)(s+4)$$

(i) modi aperiodici stabili

$$p1 = -1$$

modo  $\exp(-t)$ ,  $\tau_1 = 1$ ,  $t_{a1} = 3$

$$p2 = -4$$

modo  $\exp(-4*t)$ ,  $\tau_2 = 0.25$ ,  $t_{a2} = 0.75$

(ii)

Il modo piu' veloce è il secondo perché  $\tau_2 < \tau_1$ .

\*\*\*\*\* Es 2

$$y_f(t) = 0.5*t^2$$

\*\*\*\*\* Es 3

$$A = \begin{bmatrix} 0 & 1 \\ -6 & -5 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$C = \begin{bmatrix} 1 & 0 \end{bmatrix}$$

$$D = 0$$

Es 3.a

$$P(s) = P_{min}(s) = (s+2)(s+3)$$

Autovalori distinti ==> diagonalizzabile

\*\* Es 3.b

Matrice Modale

$$V = \begin{bmatrix} 1 & 1 \\ -2 & -3 \end{bmatrix}$$

$$V_{inv} = \begin{bmatrix} 3 & 1 \\ -2 & -1 \end{bmatrix}$$

$$A_{primo} = \begin{bmatrix} -2 & 0 \\ 0 & -3 \end{bmatrix}$$

$$B_{primo} = \begin{bmatrix} 4 \\ -3 \end{bmatrix}$$

$$C_{primo} = \begin{bmatrix} 1 & 1 \end{bmatrix}$$

$$D_{primo} = 0$$

\*\* Es 3.c

$$e_{A'}t = \begin{bmatrix} \exp(-2*t), & 0 \\ 0, & \exp(-3*t) \end{bmatrix}$$

$$e_{At} = V * e_{A'}t * inv(V) = \begin{bmatrix} 3e^{(-2t)} - 2e^{(-3t)}, & e^{(-2t)} - e^{(-3t)} \\ -6e^{(-2t)} + 6e^{(-3t)}, & -2e^{(-2t)} + 3e^{(-3t)} \end{bmatrix}$$

\*\* \*\* Es 3.d

$$x_{lib} = \begin{bmatrix} 5*\exp(-2*(t-1)) - 4*\exp(-3*(t-1)) \\ -10*\exp(-2*(t-1)) + 12*\exp(-3*(t-1)) \end{bmatrix}$$

$$y_{lib} = 5*\exp(-2*(t-1)) - 4*\exp(-3*(t-1))$$